

Lecture 7: Extensive-form game

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Contents

- So far, "Simultaneous play"
- What happens if a game is played sequentially
 - One player can see what other player chooses, and then decides on its strategy
- Equilibrium?
- What other issues?



Sequential Game

- A major class of "dynamic games", where players take their de cisions in a certain predefined order
- Role of information at each stage: very important
 - Perfect/imperfect information
- Thus, distinguish between action vs. strategy
 - Example: if an individual has to decide what to do in the evening, and the options are camping or staying at home;
 - Strategy: "If the weather report predicts dry weather for the evening, then I will go out camping; otherwise, I will stay at home"
 - Action: After knowing about the weather, the individual would take an action

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Game Trees (Extensive form)

- Extensive-form (i.e., tree)
 - Most useful representation of sequential games
 - Discrete strategy space
- Game represented as a tree
 - each non-leaf node represents a decision point for some player
 - edges represent available choices
- Can be converted to matrix game (Normal form)
 "plan of action" must be chosen beforehand



More Formal Extensive Game Definition

- An extensive form game
 - a finite set *N* of players
 - a finite height game tree
 - payoff function $u_i(s)$ for each player $i \in N$
 - where *S* is a leaf node of game tree
- Game tree: set of nodes and edges
 - each non-leaf node represents a decision point for some player
 - edges represent available choices
- Perfect information
 - all players have full knowledge of game history



Game Tree Example

 Microsoft and Mozilla are deciding on adopting new browser technology (.net or java)

- Microsoft moves first, then Mozilla makes its move



Can we look at an extensive-form game from its associated normal form game?





How should I characterize "real equilibriums" in extensive-form games?



Subgame Perfect Nash Equilibrium

- Def: a NEP is subgame perfect if its restriction to every subgame is also a NEP of the subgame
- Thr: Every extensive form game has at least one subgame perferct Nash equilibrium
 - Kuhn's theorem, based on backward induction

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What is a good algorithm to find equilibria in extensive-form game?





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Backward Induction on Game Trees

- Kuhn's Thr: Backward induction always leads to a saddle point (on games with perfect information)
 - Saddle point = subgame perfect NEP
 - game value at equilibrium is unique (for zero-sum games)
- In general, multiple NEPs are possible after backward induction

- cases with no strict preference over payoffs

- Effective mechanism to remove "bad" NEP
 - incredible threats

Summary