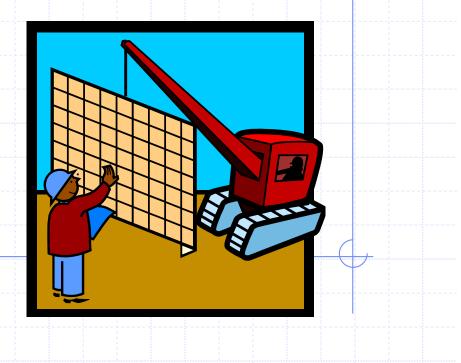
# Vector, List and Sequence

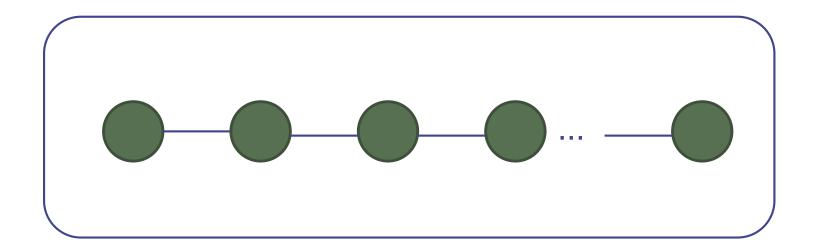


### **Overview and Reading**

Reading: Chapters: 6.1, 6.2, and 6.3

A data structure that stores n elements in a linear order

- Called list or sequence
- Didn't we learn "array" and "linked list"?
  - We are talking about more abstract ADTs than them



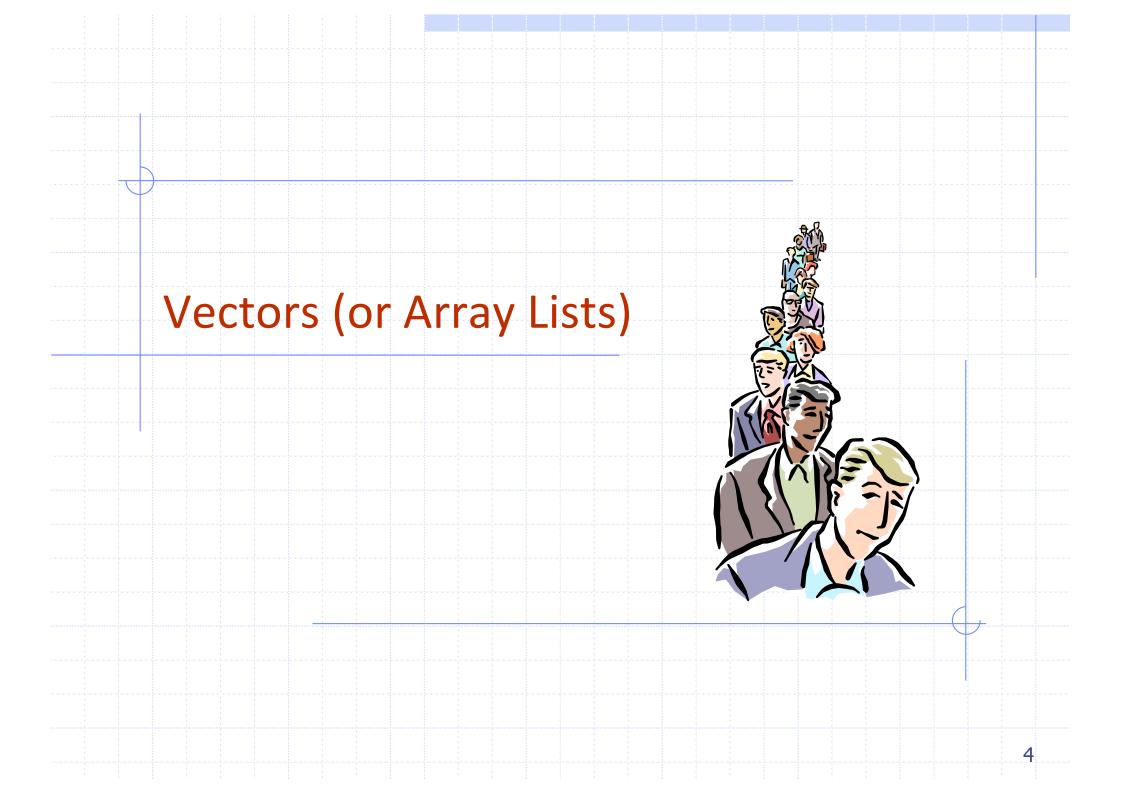
# Three ADTs

Vector (also called Array List)

- Access each element using a notion of index in [0,n-1]
- Index of element e: the number of elements that are before e
- Typically we use the "index" (e.g., [])
- A more general ADT than "array"
- 🔶 List
  - Not using an index to access, but use a node to access
  - Insert a new element e before some "position" p
  - A more general ADT than "linked list"

### Sequence

- Can access an element as vector and list (using both index and position)
- (Note) Can implement the above ADTs using various ways
  - array, singly linked list, doubly linked list, circular linked list



# The Array List ADT

- The Vector or Array List ADT extends the notion of array by storing a sequence of objects
- An element can be accessed, inserted or removed by specifying its <u>index</u> (number of elements preceding it)
- An exception is thrown if an incorrect index is given (e.g., a negative index)

### Main methods:

- at(integer i): returns the element at index i without removing it
- set(integer i, object o): replace the element at index i with o
- insert(integer i, object o): insert
   a new element o to have index i
- erase(integer i): removes element at index i
- Additional methods:
  - size()
  - empty()

# **Applications of Array Lists**

- Direct applications
  - Sorted collection of objects (elementary database)
- Indirect applications
  - Auxiliary data structure for algorithms
  - Component of other data structures
- Sasically, every place where you can use "array".

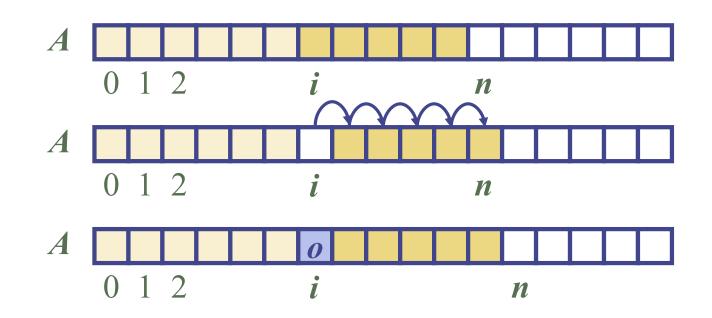
### Array-based Implementation of Vector

- $\blacklozenge$  Use an array A of size N
- A variable *n* keeps track of the size of the array list (number of elements stored)
- Operation at(i) is implemented in O(1) time by returning A[i]
- Operation set(i,o) is implemented in O(1) time by performing A[i]
   = o



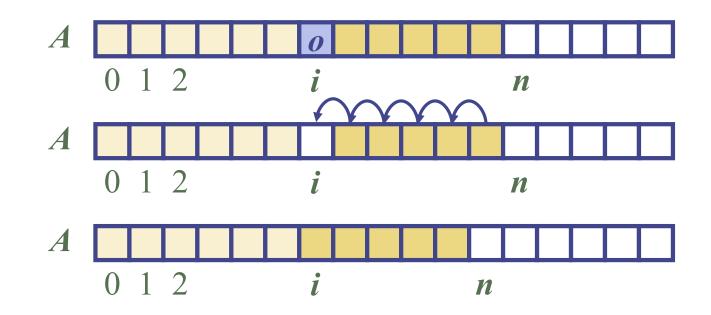
### Insertion

- ♦ In operation *insert*(*i*, *o*), we need to make room for the new element by shifting forward the n i elements A[i], ..., A[n 1]
- In the worst case (i = 0), this takes O(n) time



### **Element Removal**

- ♦ In operation *erase*(i), we need to fill the hole left by the removed element by shifting backward the n i 1 elements A[i + 1], ..., A[n 1]
- In the worst case (i = 0), this takes O(n) time



### Performance

In the array-based implementation of an array list:

- The space used by the data structure is O(n)
- *size, empty, at* and *set* run in *O*(1) time
- *insert* and *erase* run in O(n) time in worst case

• If we use the array in a circular fashion, operations *insert*(0, x) and *erase*(0, x) run in O(1) time

In an *insert* operation, when the array is full, instead of throwing an exception, we can replace the array with a larger one

### **Growable Array-based Array List**

- In an insert(o) operation (without an index), we always insert at the end
- When the array is full, we replace the array with a larger one
- How large should the new array be?
  - Incremental strategy: increase the size by a constant *c*
  - Doubling strategy: double the size

Algorithm *insert(o)* if t = S.length - 1 then  $A \leftarrow$  new array of size .... for  $i \leftarrow 0$  to n-1 do  $A[i] \leftarrow S[i]$  $S \leftarrow A$  $n \leftarrow n + 1$  $S[n-1] \leftarrow o$ 



For size n array, "re-grow" operation requires n copies

# Which is better?: Incremental or Doubling

- Comparison Method 1
  - Given the current size of S = n
  - Worst-case running time
    - Incremental strategy: O(1)
    - Doubling strategy: O(n)
- Are you happy?
  - Happy if your focus is really the worst-case
  - Unhappy
    - For doubling strategy, the total number of resizing array size would be small
- Can we reconsider the analysis method?

# Which is better?: Incremental or Doubling

- Comparison Method2
  - Compute the total time *T*(*n*) needed to perform <u>a series</u>
     <u>of *n* insert(o) operations</u>
  - Assume that we start with an empty stack represented by an array of size 1
- We call <u>amortized time</u> of an insert operation the average time taken by an insert over the series of operations, i.e., T(n)/n
  - This can be a fairer comparison in some cases
- ◆ Amortized analysis (분할상환분석 in Wiki)

### **Incremental Strategy Analysis**

We replace the old array with a new one k = n/c times
 The total time T(n) of a series of n insert operations is proportional to

$$n + c + 2c + 3c + 4c + \dots + kc =$$
  

$$n + c(1 + 2 + 3 + \dots + k) =$$
  

$$n + ck(k + 1)/2$$

• Since c is a constant, T(n) is  $O(n + k^2)$ , i.e.,  $O(n^2)$ 

• The amortized time of an insert operation is O(n)

### **Doubling Strategy Analysis**

• We replace the old array with a new one  $k = \log_2 n$  times

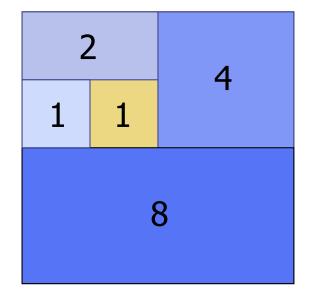
• The total time T(n) of a series of n insert operations is proportional to

$$n + 1 + 2 + 4 + 8 + \dots + 2^{k} =$$
  
 $n + 2^{k+1} - 1 =$ 

• T(n) is O(n)

• The amortized time of an insert operation is O(1)

### geometric series



### Professor, I have a question

- In "computing spans", why didn't you do amortized analysis?
   Can we do it?
- Is it meaningful?
- Think about this!
  - I am ready to discuss if you get your version of answer ready.

# Algorithm *spans2(X, n)*  $S \leftarrow$  new array of *n* integers n  $A \leftarrow$  new empty stack 1 for  $i \leftarrow 0$  to n - 1 do n while  $(\neg A.empty() \land$  $X[A.top()] \leq X[i]$  ) do *n* **A.pop()** n if *A.empty()* then n  $S[i] \leftarrow i + 1$ n else  $S[i] \leftarrow i - A.top()$ n A.push(i)n return S 1

### Vectors in C++ STL

#include <vector>
using std::vector;

// provides definition of vector
// make vector accessible

vector<int> myVector(100);

// a vector with 100 integers

- vector(n): Construct a vector with space for n elements; if no argument is given, create an empty vector.
  - size(): Return the number of elements in V.
- empty(): Return true if V is empty and false otherwise.
- resize(n): Resize V, so that it has space for n elements.
- reserve(n): Request that the allocated storage space be large enough to hold n elements.
- **operator**[i]: Return a reference to the *i*th element of *V*.
  - at(*i*): Same as V[i], but throw an out\_of\_range exception if *i* is out of bounds, that is, if i < 0 or  $i \ge V$ .size().
  - front(): Return a reference to the first element of V.
  - back(): Return a reference to the last element of *V*.
- push\_back(e): Append a copy of the element e to the end of V, thus increasing its size by one.
  - $pop\_back()$ : Remove the last element of V, thus reducing its size by one.

Difference between resize() and reserve()?

### Logistics

First programming assignment

- Deadline: Sep, 19<sup>th</sup>
- Problem Solving Homework
  - Deadline: Oct, 1<sup>st</sup>
- You should keep reading the textbook
- Sep 24<sup>th</sup>, 26<sup>th</sup> : No class
  - Thanksgiving

### Last Class

### Vector and List



- Access elements by "index"
- Incremental vs. Doubling Strategy
  - Amortized analysis



# (Node) List ADT

- The Node List ADT models a sequence of positions storing arbitrary objects
- It establishes a before/after relation between positions
- Generic methods:
  - size(), empty()

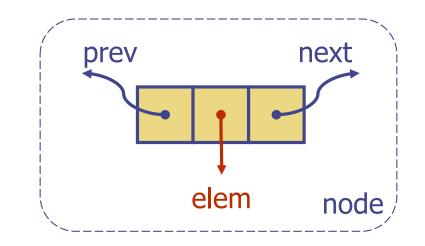
### Literators:

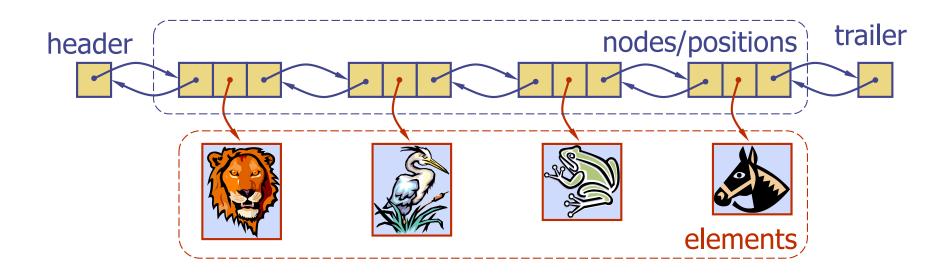
- begin(), end()
- Update methods:
  - insertFront(e),
    insertBack(e)
  - removeFront(),
    removeBack()
- □ Iterator-based update:
  - insert(p, e)
  - remove(p)

(Question) No method for accessing a specific node? We will talk about this later

### Implementation based on DLL (covered this)

- A doubly linked list provides a natural implementation of the Node List ADT
- Nodes implement Position and store:
  - element
  - link to the previous node
  - link to the next node
- Special trailer and header nodes





### Performance

- In the implementation of the List ADT by means of a doubly linked list
  - The space used by a list with *n* elements is O(n)
  - The space used by each position of the list is O(1)
  - All the operations of the List ADT run in O(1) time

### Lists in C++ STL

#include <list>
using std::list;
list<float> myList;

// make list accessible
// an empty list of floats

list(n): Construct a list with n elements; if no argument list is given, an empty list is created.

size(): Return the number of elements in *L*.

empty(): Return true if L is empty and false otherwise.

front(): Return a reference to the first element of L.

back(): Return a reference to the last element of *L*.

 $push_front(e)$ : Insert a copy of e at the beginning of L.

 $push_back(e)$ : Insert a copy of *e* at the end of *L*.

 $pop_front()$ : Remove the fist element of *L*.

 $pop_back()$ : Remove the last element of *L*.

# Containers, Iterators, and

### **Generic algorithms**



### Sorting: Vector and List

I want to find "yiyung" in Vector or List objects

vector<string> V(100); list<string> L(100); // some data insertion to V and L

//Design 1: different function
find\_vector(&V);
find\_list(&L);

//Design 2: function overloading
find(&V);
find(&L);

Do you like these? Why? Why not?

### This is how we can do in C++

```
#include <iostream>
                                                      #include <iostream>
#include <vector>
                                                     #include <list>
#include <string>
                                                     #include <string>
#include <algorithm>
                                                     #include <algorithm>
using namespace::std;
                                                     using namespace::std;
int main()
                                                      int main()
  vector<string> vec_str;
                                                       list<string> list str;
  vec_str.push_back("is");
                                                       list str.push back("is");
  vec str.push back("of");
                                                        list_str.push_back("of");
  vec str.push back("the");
                                                        list str.push back("the");
  vec str.push back("hello");
                                                        list str.push back("hello");
  vector<string>::iterator it;
                                                        list<string>::iterator it;
  it =
                                                        it =
    find(vec str.begin(), vec str.end(), "the");
                                                          find(list str.begin(), list str.end(), "the");
  cout << "Print: " << *it << endl:</pre>
                                                        cout << "Print: " << *it << endl;</pre>
  it++:
                                                        it++:
  cout << "Print: " << *it << endl;</pre>
                                                        cout << "Print: " << *it << endl;</pre>
  return 0;
                                                        return 0:
```

### It is cool. But why is it cool?

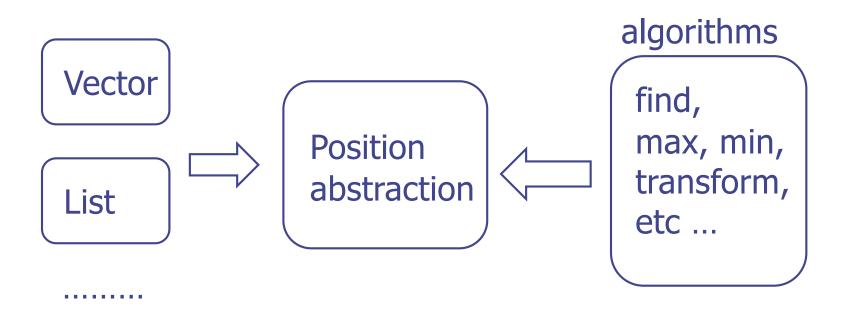
### **Mysterious things**

```
#include <iostream>
                                                      #include <iostream>
#include <vector>
                                                     #include <list>
#include <string>
                                                      #include <string>
#include <algorithm>
                                                     #include <algorithm>
using namespace::std;
                                                      using namespace::std;
int main()
                                                      int main()
  vector<string> vec str;
                                                        list<string> list str;
  vec_str.push_back("is");
                                                        list str.push back("is");
  vec str.push back("of");
                                                        list_str.push_back("of");
  vec str.push back("the");
                                                        list str.push back("the");
  vec str.push back("hello");
                                                        list str.push back("hello");
  vector<string>::iterator it;
                                                        list<string>::iterator it;
  it =
                                                        it =
    find(vec str.begin(), vec str.end(), "the");
                                                          find(list str.begin(), list str.end(), "the");
  cout << "Print: " << *it << endl:</pre>
                                                        cout << "Print: " << *it << endl;</pre>
  it++:
                                                        it++:
  cout << "Print: " << *it << endl;</pre>
                                                        cout << "Print: " << *it << endl;</pre>
  return 0;
                                                        return 0:
```

iterator? Looks like a "position" of vector or list. Hmm.....

# **Goal and Design Challenge**

- Lots of data structures (or classes in C++) that can contain various types of elements
  - "Container"
  - Examples: Vector, List, deque, set, map, etc ...



- How are you going to design this concept?
  - Again, from C++ STL designer's perspective

# **Position ADT**

- The Position ADT models the notion of place within a data structure where a single object is stored
- It gives a unified view of diverse ways of storing data, such as
  - a cell of an array
  - a node of a linked list
- "A" method of accessing the element at position p:
  - object p.element(): returns the element at position
  - In C++ it is convenient to implement this as \*p
    - Operator overloading



## Containers and Iterators in C++

- An iterator abstracts the process of scanning through a collection of elements
- A container is an abstract data structure that supports element access through iterators
  - Data structures that support iterators
  - Examples include Stack, Queue, Vector, List
  - begin(): returns an iterator to the first element
  - end(): return an iterator to an imaginary position just after the last element
- An iterator behaves like a pointer to an element
  - \*p: returns the element referenced by this iterator
  - ++p: advances to the next element
- Extends the concept of position by adding a traversal capability

### Example codes again

```
#include <iostream>
                                                      #include <iostream>
#include <vector>
                                                     #include <list>
#include <string>
                                                     #include <string>
#include <algorithm>
                                                     #include <algorithm>
using namespace::std;
                                                      using namespace::std;
int main()
                                                      int main()
  vector<string> vec str;
                                                       list<string> list str;
  vec_str.push_back("is");
                                                       list str.push back("is");
  vec str.push back("of");
                                                        list_str.push_back("of");
  vec str.push back("the");
                                                        list str.push back("the");
  vec str.push back("hello");
                                                        list str.push back("hello");
  vector<string>::iterator it;
                                                        list<string>::iterator it;
  it =
                                                        it =
    find(vec str.begin(), vec str.end(), "the");
                                                          find(list str.begin(), list str.end(), "the");
  cout << "Print: " << *it << endl:</pre>
                                                        cout << "Print: " << *it << endl;</pre>
  it++:
                                                        it++:
  cout << "Print: " << *it << endl;</pre>
                                                        cout << "Print: " << *it << endl;</pre>
  return 0;
                                                        return 0;
```

### Ah-ha, it's an iterator!

### **Various Iterators**

(standard) iterator: allows read-write access to elements

const iterator: provides read-only access to elements

bidirectional iterator: supports both ++p and -p

random-access iterator: supports both p+i and p-i

### STL Iterators in C++

Each STL container type C supports iterators:

- C::iterator read/write iterator type
- C::const\_iterator read-only iterator type
- C.begin(), C.end() return start/end iterators

This iterator-based operators and methods:

- \*p: access current element
- ++p, --p: advance to next/previous element
- C.assign(p, q): replace C with contents referenced by the iterator range [p, q) (from p up to, but not including, q)
- insert(p, e): insert e prior to position p
- erase(p): remove element at position p
- erase(p, q): remove elements in the iterator range [p, q)

### Back to Iterator: STL Iterator-based Functions

vector(p,q): Construct a vector by iterating between p and q, copying each of these elements into the new vector.

- assign(p,q): Delete the contents of V, and assigns its new contents by iterating between p and q and copying each of these elements into V.
- insert(p, e): Insert a copy of e just prior to the position given by iterator p and shifts the subsequent elements one position to the right.
  - erase(p): Remove and destroy the element of V at the position given by p and shifts the subsequent elements one position to the left.
- erase(p,q): Iterate between p and q, removing and destroying all these elements and shifting subsequent elements to the left to fill the gap.
  - clear(): Delete all these elements of V.

# **STL Containers and Algorithms**

#### #include <algorithm>

sort(p,q):	Sort the elements in the range from $p$ to $q$ in ascending order. It is assumed that less-than operator ("<") is defined for the base type.		
random_shuffle $(p,q)$ :	Rearrange the elements in the range from $p$ to $q$ in ran- dom order.		
reverse $(p,q)$ :	Reverse the elements in the range from $p$ to $q$ .		
find $(p,q,e)$ :	Return an iterator to the first element in the range from $p$ to $q$ that is equal to $e$ ; if $e$ is not found, $q$ is returned.		STL Vector STL deque
min_element $(p,q)$ :	Return an iterator to the minimum element in the range from $p$ to $q$ .		STL List
$\max_{element}(p,q)$ :	Return an iterator to the maximum element in the range from $p$ to $q$ .		
for_each $(p,q,f)$ :	Apply the function $f$ the elements in the range from $p$ to $q$ .	_	

### http://www.cplusplus.com/reference/algorithm/

### Example Code

#include <cstdlib>
#include <iostream>
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
int main () {
 int a[] = {17, 12, 33, 15, 62, 45};

// provides EXIT\_SUCCESS
// I/O definitions
// provides vector
// for sort, random\_shuffle
// make std:: accessible

vector < int> v(a, a + 6); // v: 17 12 33 15 62 45 cout << v.size() << endl;</pre> // outputs: 6 v.pop\_back(); // v: 17 12 33 15 62 cout << v.size() << endl; // outputs: 5 v.push\_back(19); // v: 17 12 33 15 62 19 cout << v.front() << " " << v.back() << endl; // outputs: 17 19 sort(v.begin(), v.begin() + 4);// v: (12 15 17 33) 62 19 v.erase(v.end() - 4, v.end() - 2); // v: 12 15 62 19 cout << v.size() << endl;</pre> // outputs: 4

# If you want to know more about iterators,

### Please watch this video

Lecture Slides for the C++ Programming Language (Version: 2016-01-18)

version. 2010-01-10)

Current with the C++14 Standard

Michael D. Adams

Department of Electrical and Computer Engineering University of Victoria Victoria, British Columbia, Canada

> University of Victoria

For additional information and resources related to these lecture slides (including errata and *lecture videos* covering the material on many of these slides), please visit: http://www.ece.uvic.ca/~mdadams/cppbook

If you like these lecture slides, *please show your support* by posting a review of them on Google Play: https://play.google.com/store/search?q=Michael%20D%20Adams%20C%2B%2B&c=books

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### https://www.youtube.com/watch?v=TxufBysSPK0

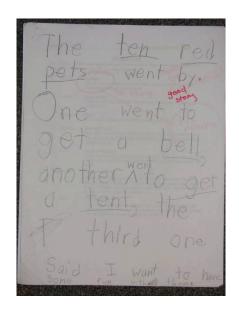


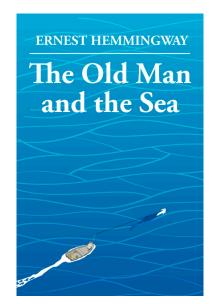
I hate to answer the question "Is this included in the exam?"

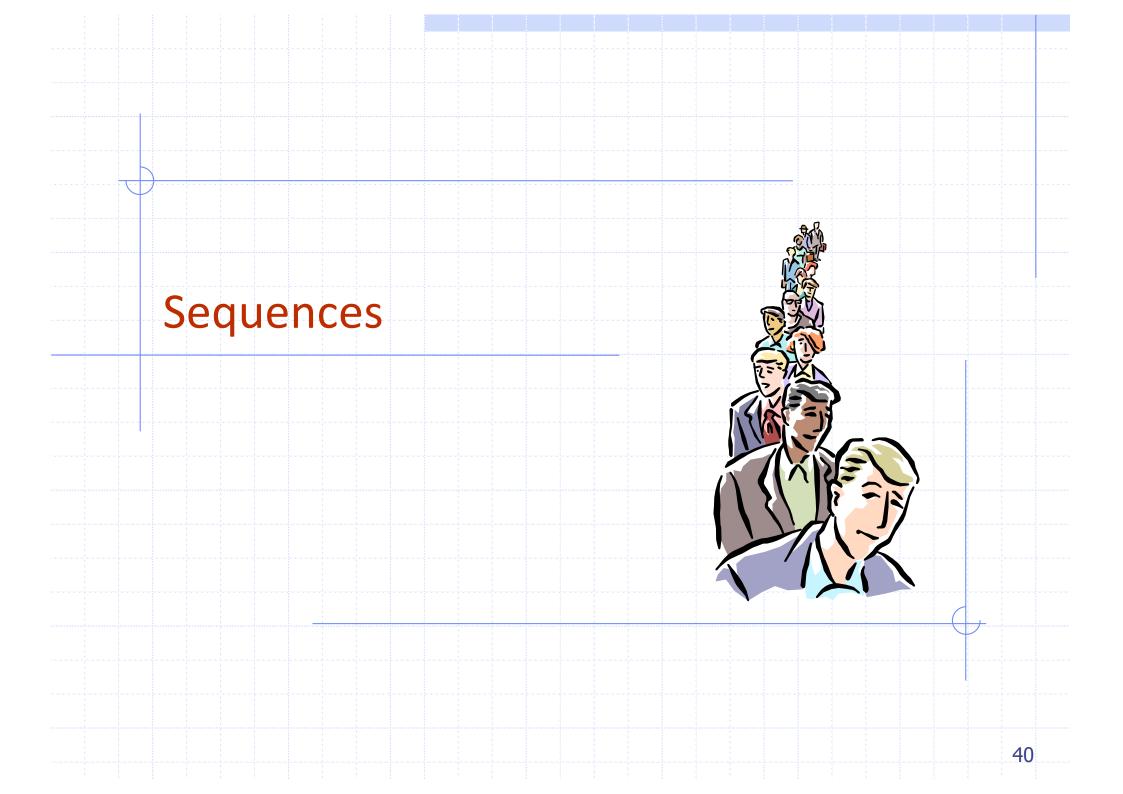
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# What should be your next question?

- Can I implement iterators in C++, in addition to just knowing how to use them?
  - Someone like the C++ STL designer
- Ch 6.2.3: Some level of explanation:
  - Beyond the topic of this class
- ◆ I will be happy to discuss this if you visit my office.







### Sequence ADT

- The Sequence ADT is the union of the Array List and Node List ADTs
- Elements accessed by
  - Index, or
  - Position
  - Generic methods:
    - size(), empty()
- ArrayList-based methods:
  - at(i), set(i, o), insert(i, o), erase(i)

- List-based methods:
  - begin(), end()
  - insertFront(o),
    insertBack(o)
  - eraseFront(),
    eraseBack()
  - insert (p, o), erase(p)
- Bridge methods:
  - atIndex(i), indexOf(p)

### **Applications of Sequences**

- The Sequence ADT is a basic, general-purpose, data structure for storing an ordered collection of elements
- Direct applications:
  - Generic replacement for stack, queue, vector, or list
  - small database (e.g., address book)
- Indirect applications:
  - Building block of more complex data structures

Questions?